

...day June 20XX – Morning/Afternoon

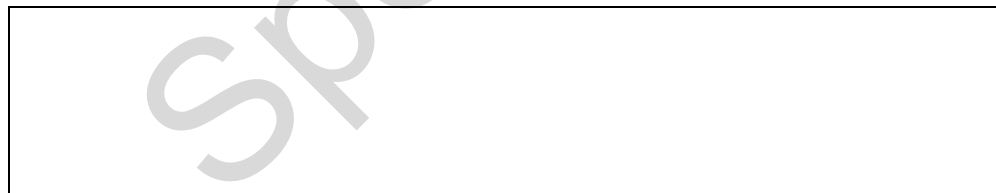
AS Level Mathematics B (MEI)

H630/01 Pure Mathematics and Mechanics

SAMPLE MARK SCHEME

Duration: 1 hour 30 minutes

MAXIMUM MARK 70



This document consists of 16 pages

Text Instructions

1. Annotations and abbreviations

| Annotation in scoris | Meaning |
|------------------------------------|---|
| ✓and ✕ | |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | Ignore subsequent working |
| M0, M1 | Method mark awarded 0, 1 |
| A0, A1 | Accuracy mark awarded 0, 1 |
| B0, B1 | Independent mark awarded 0, 1 |
| SC | Special case |
| ^ | Omission sign |
| MR | Misread |
| Highlighting | |
| | |
| Other abbreviations in mark scheme | Meaning |
| E1 | Mark for explaining a result or establishing a given result |
| dep* | Mark dependent on a previous mark, indicated by * |
| cao | Correct answer only |
| oe | Or equivalent |
| rot | Rounded or truncated |
| soi | Seen or implied |
| www | Without wrong working |
| AG | Answer given |
| awrt | Anything which rounds to |
| BC | By calculator |
| DR | This indicates that the instruction In this question you must show detailed reasoning appears in the question. |

2. Subject-specific Marking Instructions for AS Level Mathematics B

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.

- c The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be ‘follow through’. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for *g*. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate’s data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. ‘Fresh starts’ will not affect an earlier decision about a misread. Note that a miscopy of the candidate’s own working is not a misread but an accuracy error.
- i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

| Question | | | Answer | Marks | AOs | Guidance |
|----------|--|--|--------------------------------------|----------------------|--|---|
| 1 | | | $16x^8y^{-2}$ OR $\frac{16x^8}{y^2}$ | B2 [2] | 1.1 1.1 | B1 for two elements correct out of coefficient, power of x , power of y as part of a product |
| 2 | | | -15 | B3 [3] | 1.1 1.1 1.1 | B2 for 15 or $5 \times (-3)^1$ or better OR B1 for 5 or 1 5 10 10 5 1 row of Pascal's triangle seen. Do not accept ${}_5C_4$ as a correct element without evaluation to 5 |

| Question | | Answer | Marks | AOs | Guidance | | |
|----------|------|--|-------------------------------|--------------------------|--|--|--|
| 3 | (i) | E.g. The particle is in equilibrium [and the given forces cannot sum to zero as at 90°] | B1 [1] | 2.2a | oe | Accept “without another force present, the particle would be moving on a rough surface without a frictional force” | |
| 3 | (ii) | Friction 10N [to give horizontal resultant of 0] | B1 | 3.3 | oe Accept ‘Because the surface is rough’ for ‘Friction’ | | |
| | | Normal reaction from table. 8N [to give vertical resultant of 0] | B1 | 1.2 | Oe | | |
| | | Alternative method | | | | | |
| | | One extra force that gives equilibrium. Components 10 N → and 8N ↑ | B1 | 3.3 | oe Accept $\sqrt{164}$ at $\approx 39^\circ$ to horizontal | | |
| | | Components from Friction → and normal reaction ↑ | B1 | 1.2 | oe Accept ‘because the surface is rough’ for ‘Friction’ | | |
| | | | [2] | | | | |
| 4 | (i) | $(x+2)^2 + 3$ | B1 B1 [2] | 1.2 1.1 | For $b = 2$ For $c = 3$ or FT their b | | |
| 4 | (ii) | Since $(x+b)^2 \geq 0$, the minimum value [or minimum point on the curve] occurs when the expression in the bracket is zero | E1 [1] | 2.2a | | | |

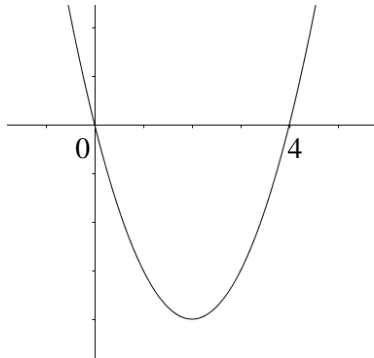
| Question | | Answer | Marks | AOs | Guidance |
|----------|------|--|-------|------|---|
| 5 | (i) | Velocity v is $\frac{ds}{dt} = 3t^2 - 6t$ | M1 | 1.1a | Attempt to find $\frac{ds}{dt}$ |
| | | $= 0$ | M1 | 1.1 | $\frac{ds}{dt} = 0$ must be stated |
| | | $t = 0$ or 2 | A1 | 1.1 | Both roots found |
| | | | [3] | | |
| | (ii) | $s(0) = 3$ so distance 3 m | A1 | 1.1 | Accept seeing 3 without comment |
| | | $s(2) = 8 - 12 + 3 = -1$ so distance is 1 m | A1 | 3.4 | -1 for s must be seen as well as 1 m for distance |
| | | | [2] | | |
| 6 | | Midpoint of $AB = (\frac{5}{2}, 0)$ | M1 | 3.1a | |
| | | Gradient of perpendicular to $AB = -\frac{1}{2}$ | M1 | 1.1 | |
| | | Perpendicular bisector equation is $y = -\frac{1}{2}(x - \frac{5}{2})$ oe | A1 | 1.1 | |
| | | Position vector is $\frac{1}{2}\mathbf{i} + \mathbf{j}$ | A1 | 1.1 | |
| | | | [4] | | |
| | | Alternative method | | | |
| | | Suppose C has position vector $\mathbf{c} = p\mathbf{i} + \mathbf{j}$ | M1 | 3.1a | |
| | | $\overline{AC} = (p-1)\mathbf{i} + 4\mathbf{j}$ oe or $ \overline{AC} ^2 = (p-1)^2 + 4^2$ oe | | | |
| | | $\overline{BC} = (p-4)\mathbf{i} - 2\mathbf{j}$ oe or $ \overline{BC} ^2 = (p-4)^2 + 2^2$ oe | M1 | 1.1 | |
| | | $(p-1)^2 + 4^2 = (p-4)^2 + 2^2$ | A1 | 1.1 | soi |
| | | Position vector is $\frac{1}{2}\mathbf{i} + \mathbf{j}$ | A1 | 1.1 | |

| Question | Answer | Marks | AOs | Guidance |
|----------|---|---|--|--|
| 7 | Find how much less distance travelled in the 50 s Distance is the area (of trapezium and is) $\frac{(25-10) \times (50+20)}{2} = 525 \text{ m}$ This distance is made up at 25 m s^{-1} to give extra time Extra time is $\frac{525}{25} = 21$ | M1 A1 M1 A1 | 3.1b 1.1 3.4 3.2a | Sensible attempt at method including finding distance as an area cao. Need not be evaluated. Many correct routes. FT their area |
| | Alternative method Find the distance travelled in the 50 s Find the time for the rest of the journey + 50 and subtract $\frac{5000}{25} = 200$ Distance travelled in the 50 s is 725 m Extra time is $\frac{(5000-725)}{25} + 50 - 200 = 21$ | M1 M1 A1 A1 [4] | 3.1b 3.4 1.1 3.2a | Sensible attempt at method including finding distance as an area May be scored later. oe cao. Many correct routes to find area FT their area. Many correct routes here. Award full marks for 21 seen www |

| Question | | Answer | Marks | AOs | Guidance |
|----------|-------|---|-----------------------------|---------------------------|---|
| 8 | (i) | Radius = 5 (2, -3) | B1 B1 [2] | 1.1 1.1 | |
| 8 | (ii) | $(y+3)^2 = 21$ or $y^2 + 6y - 12 = 0$ Roots $-3 + \sqrt{21}$ and $-3 - \sqrt{21}$ $(0, -3 + \sqrt{21})$ and $(0, -3 - \sqrt{21})$ | M1 A1 A1 [3] | 1.1a 1.1 1.1 | Substituting $x = 0$ and rearranging For one y-value All correct |
| 8 | (iii) | $(1-2)^2 + (2+3)^2 = 1^2 + 5^2$ E.g. This is more than 25 so outside the circle | M1 A1 [2] | 1.1 1.1 | Or distance of (1, 2) from their centre Or distance of (1, 2) from centre is $\sqrt{26} > 5$, so outside the circle |
| 8 | (iv) | Gradient CP = $\frac{1 - (-3)}{-1 - 2} = -\frac{4}{3}$ FT their C(entre) Gradient of tangent = $\frac{3}{4}$ FT their grad CP Equation of tangent $y - 1 = \frac{3}{4}(x - (-1))$ FT their grad $4y = 3x + 7$ oe | M1 M1 M1 A1 [4] | 1.1a 1.1 1.1 1.1 | |

| Question | | Answer | Marks | AOs | Guidance |
|----------|-------|---|---|--|--|
| 9 | (i) | $\log_{10} N = \log_{10} A + kt \log_{10} 2$ Equation above is of the form $y = mx + c$ [with $\log_{10} N$ as y and t as x] Gradient = $k \log_{10} 2$ Intercept = $\log_{10} A$ | M1 E1 A1 A1 [4] | 1.1 1.2 2.2a 2.2a | |
| 9 | (ii) | $k \log_{10} 2 = 0.2 \Rightarrow k = 0.66[438\dots]$ $\log_{10} A = 2 \Rightarrow A = 100$ | B1 B1 [2] | 1.1 1.1 | |
| 9 | (iii) | $N = 100 \times 2^{0.66 \dots \times 24} = 6\,300\,000$ FT their A, k | B1 [1] | 3.4 | Answer in range 5 860 000 to 6 400 000 |
| 9 | (iv) | E.g. the piece of bread may not be sufficient to support the number of bacteria | E1 [1] | 3.5b | OR bacterial growth may obey different rules for large values of t |

| Question | | Answer | Marks | AOs | Guidance |
|----------|------|--|-------|-------------|---|
| 10 | (i) | Correct shape for $y = \frac{1}{x}$, translated vertically upward | B1 | 1.1 | B1 for one asymptote correct |
| | | Crosses x -axis at $x = -\frac{1}{a}$ | B1 | 2.2a | |
| | | Asymptotes $x = 0$ and $y = a$ | B2 | 1.1 2.2a | |
| | | | [4] | | |
| 10 | (ii) | $\frac{dy}{dx} = -\frac{1}{x^2}$ | M1 | 1.1a | Or gradient of given line is 4 and check $4 \times -\frac{1}{4} = -1$ Or $y = \frac{5}{2}$ at the point on the curve where $x = 2$ At least one correct interim step or clear check that $\left(2, \frac{5}{2}\right)$ is on given line Any simplified form |
| | | When $x = 2$, gradient $= -\frac{1}{4}$ | M1 | 1.1 | |
| | | Gradient of normal = 4 FT their gradient | M1 | 2.1 | |
| | | $y - \frac{5}{2} = 4(x - 2)$ FT their gradient | M1 | 1.1 | |
| | | $2y = 8x - 11$ oe | A1 | 2.1 | |
| | [5] | | | | |

| Question | | Answer | Marks | AOs | Guidance |
|----------|-------|---|--|---|--|
| 10 | (iii) | $2\left(\frac{1}{x} + 2\right) = 8x - 11$ $8x^2 - 15x - 2 = 0$ Other point is $x = -\frac{1}{8}, y = -6$ | M1 M1 A1 [3] | 3.1a 1.1 1.1 | Substitution Forming quadratic, condone one error BC $x = 2$ not needed in this case |
| 11 | | DR $2x^2 - kx = x^2 - k$ $x^2 - kx + k = 0$ discriminant $= k^2 - 4k$ $k^2 - 4k \geq 0$  $k \leq 0 \text{ or } k \geq 4$ | B1 M1 B1 M1 M1 A1 [6] | 3.1a 2.1 1.2 1.1 2.4 2.5 | Equating the two expressions must be seen Condone one error in rearranging Or give table of values, oe or $\{k : k \leq 0\} \cup \{k : k \geq 4\}$ |

| Question | | Answer | Marks | AOs | Guidance |
|----------|-------|---|-------------------------------|--------------------------|------------------------------|
| 12 | (i) | No acceleration so we require the weight 15g (147N) | B1 [1] | 3.3 | Accept 15g, 15g N, 147 N etc |
| 12 | (ii) | Tension T N, N2L \uparrow $T - 147 = 15 \times 2$ So $T = 177$ and tension is 177 N | M1 A1 [2] | 3.4 1.1 | Application of N2L |
| 12 | (iii) | 177 N | B1 [1] | 3.4 | FT from (ii) |

| Question | | Answer | Marks | AOs | Guidance |
|----------|--|---|-------|-----|--|
| 12 | (iv) | Let the air resistance be $R \uparrow$ | M1 | 3.3 | Finding R using a and then T |
| | | $N2L \uparrow$ gives $R + 140 - 15g = 15 \times (-1.5)$ | M1 | 1.1 | |
| | | $R - 7 = -22.5$ | | | |
| | | $R = -15.5$ | A1 | 1.1 | |
| | | Hence magnitude is 15.5 N | A1 | 3.4 | |
| | | R is downwards so motion of the package is upwards | E1 | 3.4 | |
| | | [5] | | | |
| | | Alternative method | | | |
| | | Let the total upward force be F N and the air resistance $R \uparrow$ | | | |
| | | $N2L \uparrow$ gives $F - 147 = 15 \times (-1.5)$ | M1 | 3.3 | Finding F and hence R using a and then T |
| | | So $F = 124.5$ | A1 | 1.1 | |
| | | Also $F = R + 140$ so $R = 124.5 - 140 = -15.5$ | A1 | 1.1 | |
| | Hence magnitude is 15.5 N | A1 | 3.4 | | |
| | R is downwards so motion of the package is upwards | A1 | 3.4 | | |
| | [5] | | | | |